

# University Middle School Math Summer Work

Students entering 7<sup>th</sup> grade

Due: Friday August 21, 2020
Please Email sdmoody1@memphis.edu for any questions or help with specific sections

Unit: KNOWLEDGE of ALGEBRA, PATTERNS, and FUNCTIONS  Objective: Write an algebraic expression to represent unknown quantities.					
<ul> <li>A variable is a symbol, usually a letter, used to represent a number.</li> <li>Algebraic expressions are combinations of variables, numbers, and at least one operation.</li> </ul>					
Examples:					
The sum of 5 and some number is written as: $5 + \mathbf{n}$ becaddition.	ause the operation that is associated with the word <b>sum</b> is				
The difference of a number and three tenths is written as: word <b>difference</b> is subtraction.	n3 because the operation that is associated with the				
1.)	2.)				
a number plus $\frac{1}{2}$	a number minus .7				
3.)	4.)				
the difference of twenty-one hundredths and a number	the sum of a number and forty-six				

#### Unit: KNOWLEDGE of ALGEBRA, PATTERNS, and FUNCTIONS

Objective: Evaluate an algebraic expression.

- A variable is a symbol, usually a letter, used to represent a number.
- Algebraic expressions are combinations of variables, numbers, and at least one operation.
- Multiplication in algebra can be shown as 4n or 4 x n
- The variables in an algebraic expression can be replaced with any number.
- Once the variables have been replaced, you can evaluate, or find the value of, the algebraic expression.

#### Examples:

Evaluate 44 + n if n = 9 44 + n original expression

44 + 9 replace the variable with it's value

53 solution

1.)

Evaluate 150 + n if n = 15

Evaluate 12n if n = 9

3.)

Evaluate 15n + 19 if  $n = \frac{1}{3}$ 

Evaluate 30n if n = 2.5

5.)

Evaluate  $24n \div k$  if n = 6 and k = 8

Evaluate nk - 2b + 8 if b = 1.5, k = 8, and n = 7

## Unit: KNOWLEDGE of ALGEBRA, PATTERNS, and FUNCTIONS

**Objective:** Evaluate numeric expressions using order of operations.

- A numerical expression is a combination of numbers and operations.
- The **Order of Operations** tells you which operation to perform first so that everyone gets the same final answer.
- The Order of Operations is: Parentheses, Exponents, Multiplication or Division (left to right), and Addition or Subtraction (left to right.)

#### Examples:

$$48 \div (3 + 3) - 2^2$$
 original expression

$$48 \div 6 - 2^2$$
 simplify the expression inside the parentheses

$$48 \div 6 - 4$$
 calculate  $2^2$   $8 - 4$  divide  $48$  by  $6$  subtract 4 from  $8$ 

$$(8 + 1) \times 12 - 13$$
  $13 \times 4 - 72 \div 8$ 

$$88 - 16 \times 5 + 2 - 3$$
  $100 \div 5^2 \times 4^3$ 

$$45 \div 9 - 3 + 2 \times 3$$
  $(5^2 + 3^3) \times (81 + 9) \div 10$ 

## Unit: KNOWLEDGE of ALGEBRA, PATTERNS, and FUNCTIONS

**Objective:** Determine the unknown in a linear equation (addition & subtraction).

- Addition equations: Subtract the same number from each side of the equation so that the two sides remain equal.
- Subtraction equations: Add the same number to each side of the equation so that the two sides remain equal.

#### Examples:

$$b + 3 = 6$$
 original equation 
$$b - 8 = 4$$
 original equation 
$$b + 0 = 3$$
 subtract 3 from each side 
$$b + 0 = 3$$
 solution 
$$b = 3$$
 simplify 
$$b = 12$$
 simplify

1.)

$$g + 5 = 12$$
  $s - 12 = 29$ 

3.)

$$m + 3.5 = 10.5$$
  $k - 5.5 = 8.5$ 

5.) w + 6.25 = 22 g - 3.75 = 49.75

## Unit: KNOWLEDGE of ALGEBRA, PATTERNS, and FUNCTIONS

Objective: Determine the unknown in a linear equation (multiplication & division).

- In a **multiplication equation**, the number by which a variable is multiplied is called the **coefficient**. In the multiplication equation 2x = 8, the coefficient is 2.
- Multiplication equations: Divide both sides by the coefficient so that the two sides remain equal.
- In a **division equation**, the number by which the variable is divided is called the **divisor**. In the division equation  $\frac{x}{4}$ , 4 is the divisor.
- Division equations: Multiply both sides of the equation by the divisor so that the two sides remain equal.

## Examples:

4b = 16	original equation	$\frac{m}{6} = 11$	original equation
4 4	divide both sides by 4	$6 \times \frac{m}{6} = 11 \times 6$	multiply each side by 6
1b = 4 b = 4	solution simplify	1m = 66 m = 66	solution simplify

1.) 7x = 63 2.)  $\frac{k}{9} = 8$ 

3.)

 $\frac{n}{7} = 5.55$ 

5.)  $\frac{p}{13} = 2.67$ 

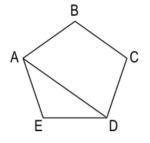
#### Unit: KNOWLEDGE of GEOMETRY

Objective: Identify and describe diagonal line segments.



• A line segment connecting two vertices of a polygon is either a side or a diagonal.

Examples:

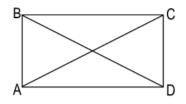


 $\overline{AE}$  is a side of polygon ABCDE

 $\overline{AD}$  is a **diagonal** of polygon ABCDE

1.)

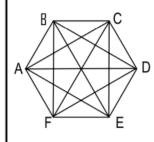
Is  $\overline{AB}$  a diagonal of polygon ABCD?



YES NO

2.)

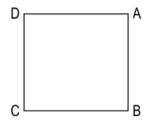
Circle all of the diagonals of polygon ABCDEF.



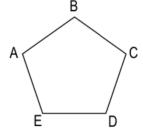
ABAEAFADBABCBDBEBF $\overline{CB}$  $\overline{CD}$   $\overline{CE}$   $\overline{CF}$ CADE DFDADBDCEBEDEFFD FE

3.)

Name one diagonal of polygon WXYZ

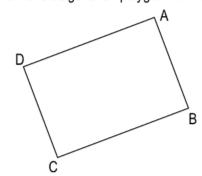


**4.)**Name all of the diagonals polygon *ABCDE* 

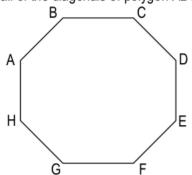


5.)

Draw one diagonal on polygon KLMN



**6.)** Draw all of the diagonals of polygon *ABCDEFGH* 



#### Unit: KNOWLEDGE of GEOMETRY

Objective: Compare or classify triangles as scalene, equilateral, or isosceles.

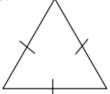


**Triangles** are polygons that have **three sides**, three vertices, and three angles.

Triangles can be classified by the number of congruent sides, which are sides of equal length.

The same markings on the sides of a triangle show that the sides are **congruent**.

Examples:



Equilateral triangle Three congruent sides



Isosceles triangle Two congruent

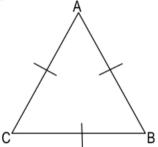


Scalene triangle No congruent sides

1.) Shown is Equilateral triangle ABC.

$$\overline{AB}$$
 = 6 cm.

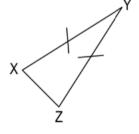
$$\overline{BC} =$$



2.) Shown is Isosceles triangle XYZ.

$$\overline{XY} = 5 \text{ in.}$$

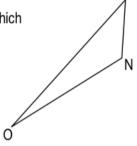
What must be the length of side  $\overline{YZ}$ ?



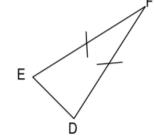
3.) Shown is Scalene triangle MNO.

Circle the set of numbers which could be the lengths of the three sides.

3 cm, 5 cm, 6 cm 2 cm, 4 cm, 4 cm 2 cm, 2 cm, 2 cm



4.) Classify triangle DEF.



Equilateral

Scalene

Isosceles

- **5.)** Draw an Equilateral triangle. Label the vertices. Name the sides and their lengths.
- **6.)** Draw a Scalene triangle. Label the vertices. Name the sides and their lengths.

## **Grade - Summer Math Packet**

Unit: KNOWLEDGE of GEOMETRY

Objective: Compare or classify triangles as equiangular, obtuse, acute, or right.



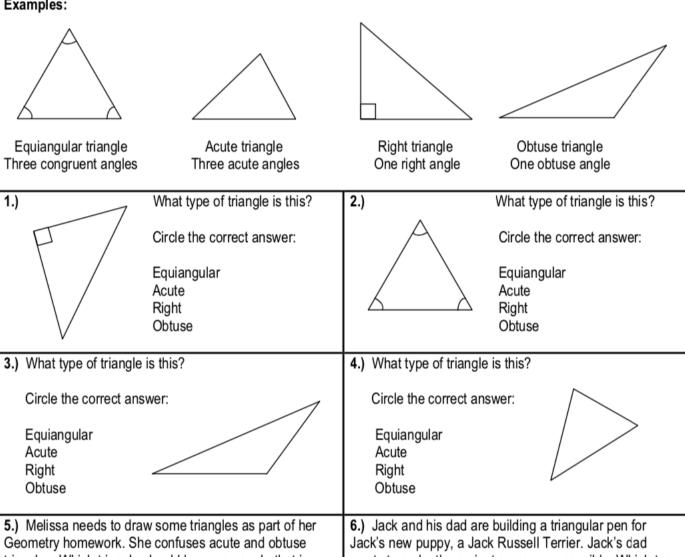
**Triangles** are polygons that have three sides, three vertices, and **three angles**.

Triangles can be classified according to their angles.

All triangles have at least 2 acute angles. Acute, Right, and Obtuse triangles are classified according to their third angle.

The same markings on the angles of a triangle show that the angles are **congruent**.

#### Examples:



wants to make the project as easy as possible. Which type of triangle should they use as a model? Why?

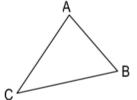
#### Unit: KNOWLEDGE of GEOMETRY

**Objective:** Use the concept of the sum of angles in any triangle is 180° to determine the third angle measure of a triangle given two angle measures without a diagram.



**Triangles** are polygons that have three sides, three vertices, and **three angles**. The **sum** of the measures of the angles of a triangle is **180°**.

Examples:



Angle A = 
$$65^{\circ}$$
  
Angle B =  $60^{\circ}$   
Angle C = ?

$$180 - 65 - 60 = 55$$
 Angle C =  $55^{\circ}$ 

**1.)** Given triangle XYZ:

2.) Given triangle MNO:

Angle 
$$O = 135^{\circ}$$

3.) Given right triangle ABC:

Angle A is the right angle

4.) Given equiangular triangle FGH:

What is the measure of ...

Angle F? \_\_\_\_°

Angle G? \_\_\_\_\_°

Angle H? \_\_\_\_\_°

**5.)** Given triangle JKL:

Angle 
$$J = 120^{\circ}$$

Angle L = 
$$20^{\circ}$$

Is this possible? Explain why or why not using math.

**6.)** Teri is making a scrapbook page of her trip to the art exhibit, "Geometry in Your World." She wants to use a large triangle as her background focus. She draws a triangle with the first two angle measures of 100° and 25°.

What is the angle measure of the third angle? \_\_\_\_\_°

Please show your work:

#### Unit: KNOWLEDGE of GEOMETRY

**Objective:** Identify, or describe angle relationships using perpendicular bisectors or angle bisectors.



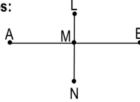
To **bisect** something means to separate it into **two equal parts**.

When a line segment is bisected with a perpendicular line segment, you have two line segments that are congruent (or equal in length.)

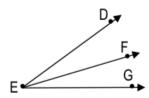
The original line segment and the perpendicular line segment meet at right (90°) angles.

When an angle is bisected, the resulting two angles are congruent.

Examples:



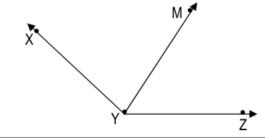
Line segment  $\overline{LN}$  is the perpendicular bisector of line segment  $\overline{AB}$ , so line segment  $\overline{AM}$  is congruent to line segment  $\overline{MB}$ . Angle LMB is 90°.



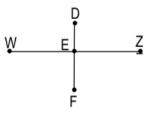
Ray  $\overrightarrow{EF}$  is the bisector of angle DEG, so angle DEF is congruent to angle FEG.

**1.)** Given angle XYZ and bisector  $\overrightarrow{YM}$ , name the 2 angles that are congruent.

Angle \_\_\_\_\_ and angle \_\_\_\_ are congruent.



3.)



Line segment  $\overline{WZ}$  is the original line segment.

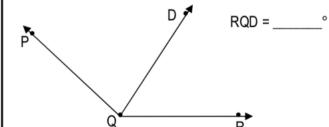
Line segment  $\overline{DF}$  is the \_\_\_\_\_\_.

Line segments  $\overline{EW}$  and  $\overline{EZ}$  are \_\_\_\_\_.

The measure of angle WEF is \_\_\_\_\_°.

**2.)** Angle PQR measures 124°. Ray  $\overrightarrow{QD}$  bisects angle PQR. What is the measure of angle DQR and angle RQD?

DQR = \_\_\_\_\_°



4.)



Name the perpendicular bisector: \_\_\_\_\_

Name the 2 congruent line segments: \_\_\_\_\_ & \_\_\_\_

Name all of the right angles:

If line segment  $\overline{MB}$  = 9 mm, then line segment  $\overline{AB}$  = \_\_\_\_\_

# Unit: KNOWLEDGE of MEASUREMENT Objective: Measure length to the nearest 1/16 inch using a ruler. You will need a ruler for this lesson! \*\*Note: This ruler is NOT to <u>15</u> 16 scale. Examples: Measure the following objects to the nearest 1/16 inch. 0 in Paperclip = $\frac{3}{4}$ inch Pencil = $\frac{15}{16}$ inch Measure the objects to the nearest 1/16 inch. 1.) 2.) 4.) 3.) 5.) 6.)

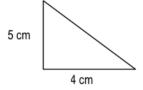
#### Unit: KNOWLEDGE of MEASUREMENT

**Objective:** Estimate and determine the area of a triangle with whole number dimensions.



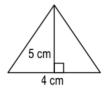
The area (**A**) of a triangle is one half the product of the base (**b**) and the height (**h**). The formula for finding the area of a triangle is: **A** =  $\frac{1}{2}$  **bh** and is measured in square units.

Examples:



$$A = \frac{1}{2} bh$$
  $A = \frac{1}{2} x 4 x 5$   $A = \frac{1}{2} x 20$ 

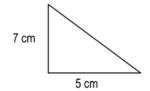
 $A = 10 \text{ cm}^2$ 



$$A = \frac{1}{2} bh$$
  $A = \frac{1}{2} x 4 x 5$   $A = \frac{1}{2} x 20$ 

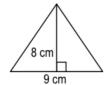
 $A = 10 \text{ cm}^2$ 

1.) Determine the area of the triangle.



$$A = cm^2$$

**2.)** Determine the area of the triangle.



**3.)** Determine the area of an obtuse triangle with a height of 11 cm and a base of 22 cm.

A = \_\_\_\_\_

**4.)** Determine the area of an isosceles triangle with a base of 13 cm and a height of 26 cm.

**5.)** World famous pastry chef, Chen Lee, is designing a birthday cake for his son, who is a Geometry teacher. He has 4 layers, all triangles. He wants to put the largest layer (in area) on the bottom and the smallest layer on the top. Determine the area of each layer and order them from largest to smallest (4 = largest, 1 = smallest)

\_\_\_ Milk Chocolate layer b = 12" h = 6" A =

\_\_\_ Yellow cake layer b = 7" h = 11" A =

\_\_ Dark Chocolate layer b = 4" h = 17" A =

\_\_\_ White cake layer b = 9" h = 9" A =

**6.)** Natasha's dorm room is shaped like a triangle. The college brochure says it has an area of 875 square feet. The room is 35 feet long. Determine the width of the room at its widest point.

#### Unit: KNOWLEDGE of MEASUREMENT

Objective: Estimate and determine the volume of rectangular prisms with whole number dimensions.

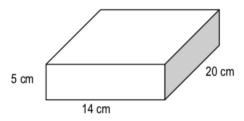


The amount of space inside a three-dimensional figure is the **volume** of the figure.

Volume (V) is measured in cubic units.

The volume of a rectangular prism is related to its dimensions. Volume (V) = length (I) x width (w) x height (h)

#### Examples:

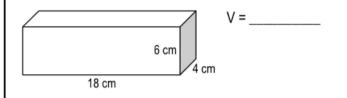


$$V = I \times w \times h$$

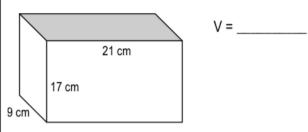
$$V = 20 \times 14 \times 5$$

$$V = 1400 \text{ cm}^3$$

**1.)** Determine the volume of the rectangular prism. Please show your work.



**2.)** Determine the volume of the rectangular prism. Please show your work.



- **3.)** Determine the volume of a rectangular prism with a length of 13 cm, a width of 55 cm, and a height of 65 cm. Please show your work.
- **4.)** Determine the volume of a rectangular prism with a height of 35 cm, a length of 89 cm, and a width of 15 cm. Please show you work.
- **5.)** Tyrone has a fish tank that measures 36 in. long, 24 in. high, and 18 in. wide. He wants to fill the fish to a height of 14 inches. What will be the volume of water in the tank? Please show your work.



Draw the tank and label the dimensions. Draw the water level. This does not need to be drawn to scale.

**6.)** Shanika has a lamp that she wants to send to her sister in Baltimore. The lamp is in the shape of a rectangular prism. It measures 14" high, 9" wide, and 3" long. She wants to buy a box so that there is 1" all around the lamp for bubble wrap.

What should be the dimensions of the box?

What is the volume of the box? Please show your work.

#### Unit: KNOWLEDGE of MEASUREMENT

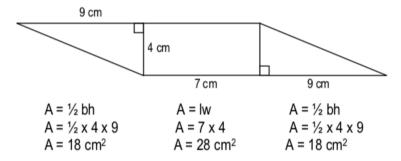
**Objective:** Estimate and determine the area of composite figures using no more than four polygons (triangles or rectangles) with whole number dimensions.



A composite figure is made by combining two different figures.

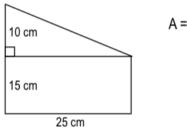
The area of a composite figure is found by adding the areas of the individual figures.

Examples:



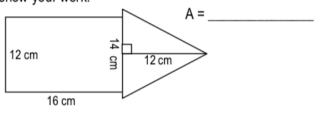
Area of composite figure = 18 + 28 + 18 = 64 cm<sup>2</sup>

**1.)** Determine the area of the composite figure. Please show your work.

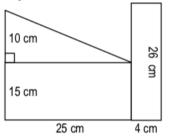


A = \_\_\_\_\_

**2.)** Determine the area of the composite figure. Please show your work.



**3.)** Determine the area of the composite figure. Please show your work.



A = \_\_\_\_\_

**4.)** Determine the area of the composite figure that is made up of 1 square and 3 congruent right triangles. Each triangle shares its base with one side of the square. One side of the square measures 6cm. The height of each triangle is 4 times its base. Please show your work.

**5.)** Dallas is working on the decorations for the 8th grade dance. He is making a large composite wall decoration that is made of 2 congruent rectangles and 2 congruent triangles. The rectangles measure 5 ft by 7 ft. The triangles have a base of measurement of 7 ft and a height measurement of 9 ft. What is the composite area of the wall decoration?

What is the composite area of 4 of them?

**6.)** The 8<sup>th</sup> grade dance committee liked Dallas' decorations so much that they decided to paint a huge one on the floor. They tripled the dimensions of the rectangles and the triangles?

What is the area of the floor decoration?

#### Unit: KNOWLEDGE of MEASUREMENT

**Objective:** Determine the missing side of a quadrilateral given the perimeter using whole number dimensions.

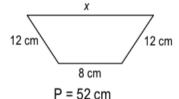


A quadrilateral is any four-sided, closed, 2-dimensional figure.

The **perimeter (P)** of any quadrilateral is the sum of the lengths of its four sides.

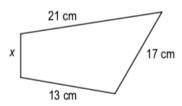
The missing side of a quadrilateral can be found using addition and subtraction.

Examples:

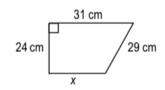


P = 
$$s + s + s + s$$
  
 $52 = 12 + 8 + 12 + x$   
 $52 = 32 + x$   
 $\frac{-32}{20 = x}$  The length of the missing side is 20 cm.

**1.)** Determine the missing side of the quadrilateral. Please show your work.



**2.)** Determine the missing side of the quadrilateral. Please show your work.



$$P = 99 \text{ cm}$$

**3.)** Determine the missing side of the quadrilateral. Please show your work.





**4.)** Determine the missing side of a quadrilateral that has a perimeter of 251 cm and three sides measuring 39 cm, 72 cm, and 89 cm. Please show your work.

**5.)** Heather wants to build a pen for her new beagle puppy. She is going to build it in the shape of a quadrilateral. She decides that she wants the perimeter to be 360 ft. She already has 360 feet of fence. She measures out the first side to be 90 ft, the second side to be 110 feet, and the third side to be 100 feet. She tells her friend to measure out the fourth side to be 80 feet.

Is this correct? Why or why not? Please show your work.

**6.)** Michael is designing a corn maze for his grandfather's farm. The general shape of the corn maze is a quadrilateral. The perimeter of the corn maze is 1,221 feet. The top measures 381 feet. The bottom measures 227 feet. One of the sides measures 294 feet.

Determine the length of the other side. \_\_\_\_\_

Is this missing side shorter or longer than the other side? Please show your work to prove your answer.

#### Unit: KNOWLEDGE of MEASUREMENT

**Objective:** Determine the missing measure of a square or rectangle given the area using whole number dimensions.



The area (A) of a rectangle or square can be found by multiplying the length (I) by the width (w).  $A = I \times W$  The missing measure of a square or rectangle can be determined by using division.

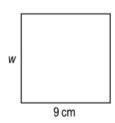
## Examples:

$$A = 1 \times w$$
  
 $64 = 16 \times w$   
 $16 = 16 \times w$ 

 $A = 64 \text{ cm}^2$ 

4 = w The width of the rectangle is 4 cm.

**1.)** Determine the missing side of the square. Please show your work.



$$A = 81 \text{ cm}^2$$

w=

**2.)** Determine the missing side of the rectangle. Please show your work.



$$A = 65 \text{ cm}^2$$

/=

**3.)** Determine the missing side of a rectangle with an area of 144 cm<sup>2</sup> and a width of 8 cm. Please show your work.

**4.)** Determine the missing side of a rectangle with an area of 480 cm<sup>2</sup> and a length of 32 cm. Please show your work.

**5.)** Marcus plans to paint a bright green rectangle on the bottom of his pool. He has enough paint to cover an area of 273 square feet. He wants the width of the rectangle to be 13 feet. Determine what the length of the rectangle should be. Please show your work.

**6.)** Brianna wants to put stickers, to celebrate her birthday, on top of chocolate bar wrappers. The bar is 48 mm wide and has an area of 4128 mm<sup>2</sup>. What must be the length of the sticker to cover the top of the bar?

#### Unit: KNOWLEDGE of STATISTICS

**Objective:** Organize and display data to make frequency tables with no more than 5 categories or ranges of numbers and total frequencies of no more than 25.



Statistics involves collecting, organizing, analyzing, and presenting data.

**Data** are pieces of information that are often numerical.

Data can be organized in a frequency table, which shows the number of pieces of data that fall within given intervals.

**Examples:** The grades scored on a geometry quiz are shown in the table. Make a frequency table of the data.

Geometry Quiz Scores							
99	83	92	52	75			
90	99	65	80	85			
53	80	75	85	85			
70	75	90	95	75			

Geometry Quiz Scores			
Scores	Tally	Frequency	
51 – 60	II	2	
61 – 70	II	2	
71 – 80	JH I	6	
81 – 90	JJK I	6	
91 - 100	IIII	4	

1.) The owners of Donut Delight want to move their store to a new location. They asked their customers in which general direction they lived from the store. The data is shown in the table. Make a frequency table of the data.

9	<u>Customer Locations</u>						
Ν	S	Е	S	N	W		
Ε	Ν	W	S	Ν	Ν		
W	Ε	S	Ε	Ν	Ε		
S	Ν	Ν	W	S	Ε		

Customer Locations				
Direction	Tally	Frequency		
North				
East				
South				
West				

2.) Ms. Wolf asked her students to name their favorite food. The data is shown in the table. Make a frequency table of the data.

Favorite foods						
C D P H	T C H P	H H D T	P T T T	P P C	C P T P	

#### Unit: KNOWLEDGE of STATISTICS

**Objective:** Interpret frequency tables with no more than 5 categories or ranges of numbers and frequencies of no more than 25.



The data in a frequency table can be analyzed and interpreted by comparing the frequencies in each category.

**Examples:** Maria is counting three types of insects she finds under rocks in the park for an ecology survey. Her data is shown in the frequency table.

Insects Under a Rock				
Insects	Frequency			
Beetle	וו אול אוז אוז	17		
Earwig	ו אוז אוז אוז אוז	21		
Spider	în III	8		

How many more Earwigs did Maria find than Beetles? 21 – 17 = 4 more Earwigs

How many less spiders did Maria find than Beetles? 17 - 8 = 9 less Spiders

In her report Maria is going to list the insects in order of most common to least common. What order should she write in her report? **Earwig (21), Beetle (17), Spider (8)** 

1.) The frequency table shows the number of hours the band members in Mrs. Robinson's class practiced last week.

Practice Hours			
Hours	Hours Tally		
0	I	2	
1	וווו ואר את וווו	19	
2	IN IN I	11	
3	M II	7	
4	III	3	

How many students practiced more than 2 hours?

How many students practiced either 1 or 2 hours?

List the hours practiced from least common to most common.

2.) The frequency table shows Mr. Helta's students' favorite flavor if ice cream.

How many more students liked Chocolate than Chocolate Chip?

How many less students liked Strawberry than Chocolate and Vanilla?

The same amount of students liked Chocolate and Strawberry as did those who liked \_\_\_\_\_ and .

Favorite Flavors of Ice Cream				
Flavor Tally Frequency				
Vanilla	INI I	6		
Chocolate IN IIII		9		
Strawberry	I	1		
Cookies 'n Cream	ו או או	11		
Chocolate Chip	IIII	4		

#### Unit: KNOWLEDGE of STATISTICS

**Objective:** Organize and display the data for a given situation to make stem and leaf plots using no more than 20 data points and whole numbers.



In a stem-and-leaf plot, the data is ordered from least to greatest and is organized by place value.

The digits in the left hand column are the stems. Each digit on the right is called a leaf.

A key must be included that explains the stems and leaves.

#### Examples:

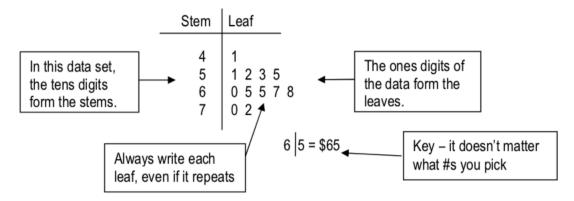
Money Earned Mowing Lawns (\$)					
60	55	53	41		
67	72	65	68		
65	70	52	51		

Step 1: Order the data from least to greatest: 41 51 52 53 55 60 65 65 67 68 70 72

Step 2: Draw a vertical line and write the tens digit from least to greatest to the left of the line.

Step 3: Write the ones digits to the right of the line with the corresponding stems.

Step 4: Include a key that explains the stems and leaves.



- 1.) Make a stem-and-leaf plot for this data: 34 44 51 48 55 41 47 44 22 55 33
- **2.)** Make a stem-and-leaf plot for this set of data: \$52 \$49 \$37 \$21 \$65 \$49 \$23 \$51 \$22 \$21 \$61

- **3.)** Barbara counted the number of butterflies that visited her butterfly garden each hour. Make a stem-and-leaf plot of her data. 18 24 50 29 19 34 42 34 45 34 50 47
- **4.)** Here are Ms. Corio's students' scores on their last math test. Make a stem-and-leaf plot of her data.

98 83 91 101 87 62 93 87 79 72 98 100 77 87 99

#### Unit: KNOWLEDGE of STATISTICS

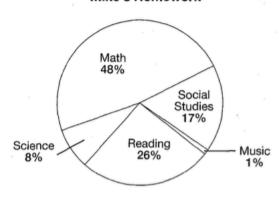
**Objective:** Interpret circle graphs using no more than 5 categories and whole numbers or percents.



A circle graph is used to compare parts of a whole.

#### **Examples:**

#### Mike's Homework



Which subject does Mike spend most of his time on? Math

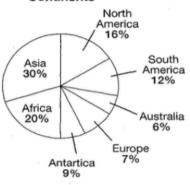
How does the time spent on reading compare to the time spent on social studies? 26 - 17 = 9 He spends 9% more time on reading.

On which subject does Mike spend almost as much time on as he does social studies and science combined? 17+ 8 = 25 Mike spends 26% on reading; almost equal to 25%.

Mike's mom wants to know how he spends his homework time. Order the subjects from most time spent to least time spent. **Math, Reading, Social Studies, Science, Music** 

1.) The circle graph show how much of the Earth's land each continent represents.

#### Continents



What continent has the greatest area?

Which two continents are the smallest?

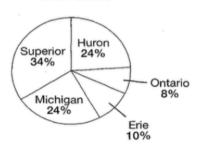
How does the size of Europe compare to the size of Africa?

How much larger is Asia than North America?

List the continents from smallest to largest.

2.) The circle graph shows how much of the total surface of the Great Lakes each lake takes up.

#### **Great Lakes**



Which of the Great Lakes is the smallest?

Which two lakes are about the same size?

How does Lake Erie compare to Lake Ontario?

Which two lakes together are the same size as Lake Superior?

Which of the Great Lakes is the largest?

#### Unit: KNOWLEDGE of STATISTICS

Objective: Determine the measures of central tendency (mean, median, and mode) and the range.



A number that helps describe all of the data in a data set is a measure of central tendency.

The **mean** is the sum of the data divided by the number of pieces of data.

The **median** is the middle number of the ordered data (least to greatest.)

The **mode** is the number or numbers that occur most often.

The range is the difference between the greatest and least values of the data set.

#### Examples:

Find the mean, median, mode, and range of the data.

Mean = 
$$25 + 34 + 39 + 41 + 45 + 52 + 27 + 22 + 56 + 61 + 15 + 27$$
  
12  
=  $444$  = 37 The mean price of a jacket is \$37.

Median = 15 22 25 27 27 34 39 41 45 52 56 61 (data ordered)

$$=$$
  $\frac{34 + 39}{2}$  = **36.5** The median price of a jacket is \$36.50.

Mode = \$27 because it is the only piece of data that occurs more than once.

Range = 
$$61 - 15 = $46$$

1.) Find the mean, median, mode, and range for	each set
of data.	

6, 9, 2, 4, 3, 6, 5

**2.)** Find the mean, median, mode, and range for each set of data.

13, 7, 17, 19, 7, 15, 11, 7, 21

28, 32, 23, 43, 32, 27, 21, 34

**4.)** Find the mean, median, mode, and range for each set of data.

157, 124, 157, 124, 157, 139

## Unit: NUMBER RELATIONSHIPS and COMPUTATION **Objective:** Read, write, and represent integers. Examples: **Integer:** Any number from the set {... -3,-2,-1,0,1,2,3...} Integers less than zero Integers greater than zero are negative integers are positive integers -3 -2 -1 3 5 6 -5 Positive integers can be written Negative integers are Zero is neither nor positive written with a - sign with or without a + sign Write an integer to describe each situation a height increase of 3 inches The word increase represents positive. The integer is 3 or +3. EX: 50 feet below sea level The word below represents negative. The integer is -50. Write an integer to describe: 1.) 2.) Write an integer to describe: The stock market increased 75 points A loss of 15 yards Write an integer to describe the situation: 3.) 4.) Write an integer to describe: Nancy owes her friend \$10 Frederick is located 290 feet above sea level. 5.) Write an integer to describe: 6.) Write an integer to describe: The temperature was 3° below zero The 6th grade has 12 fewer students than last year

## Unit: NUMBER RELATIONSHIPS and COMPUTATION

Objective: Identify and determine equivalent forms of proper fractions as decimals, percents, and ratios - A.

**Examples:** Write  $\frac{21}{25}$  as a decimal

## Method 1:

Change  $\frac{21}{25}$  to a fraction with a denominator of 10, 100, or 1000

**EX:** 
$$\frac{21}{25} = \frac{?}{100}$$

(Use 100, since 25 divides into 100 evenly)

$$\frac{21}{25} = \frac{x4}{x4} = \frac{84}{100}$$
  $\frac{84}{100} = 0.84$  as a decimal

Method 2: Divide 21 by 25

$$\frac{21}{25} \longrightarrow 25 )21.00$$

$$-200$$
100
$$-100$$

Therefore:  $\frac{21}{25} = 0.84$ 

1.) Write 
$$\frac{19}{20}$$
 as a decimal. Use method 1

**2.)** Write  $\frac{7}{8}$  as a decimal. Use method 2.

3.) Write 
$$\frac{3}{16}$$
 as a decimal. Use method 2

**4.)** Write  $\frac{27}{40}$  as a decimal. Use method 2

**5.)** Write 
$$\frac{3}{4}$$
 as a decimal. Use method 1

6.) Write  $\frac{3}{5}$  as a decimal. Use method 1

#### Unit: NUMBER RELATIONSHIPS and COMPUTATION

Objective: Identify and determine equivalent forms of proper fractions as decimals, percents, and ratios - B.

Key Concept: Percent (%) is a ratio that compares a number to 100

## **Fraction to Percent:**

**EX:** Change  $\frac{19}{25}$  to a percent

Since % means out of 100,  $\frac{19}{25} = \frac{?}{100}$ 

$$\frac{19}{25} = \frac{x4}{x4} = \frac{76}{100}$$
$$\frac{76}{100} = 76\%$$

Percent to fraction:

EX: Change 75% to a fraction in simplest form

75% means 75 out of 100

 $75\% = \frac{75}{100}$  Write the percent as a fraction with a denominator of 100

$$\frac{75}{100} \div \frac{25}{25} = \frac{3}{4}$$
 Simplify

1.) Change  $\frac{17}{20}$  to a percent

2.) Change 84% to a fraction in simplest form

3.) Change  $\frac{3}{4}$  to a percent

4.) Change 90% to a fraction in simplest form

- **5.)** Juan answered  $\frac{24}{25}$  questions correctly on his quiz. What percent of the questions did he get correct?
- 6.) 78% of the class completed their homework last night. What fraction of the class completed their homework?

/ Grade - Summer Wath Facket				
Unit: NUMBER RELATIONSHIPS and COMPUTATION Objective: Identify and determine equivalent forms of proper fractions as decimals, percents, and ratios - C.				
Key Concept: Ratio: a comparison of two numbers A ratio can be written in 3 ways: a:b a to b or a b				
EX: Write the ratio as a fraction simplest form: 4 wins to 6	losses			
Since the ratio can be written as: $\frac{4}{6}$ we can the simplify to $\frac{2}{3}$ or 2:3 or 2 to 3				
1.) Write the ratio as a fraction simplest form:  12 boys to 15 girls	2.) Write the ratio as a fraction simplest form:  20 books to 24 magazines			
3.) Write the ratio as a fraction simplest form:  10 circles to 15 triangles	4.) Write the ratio as a fraction simplest form: 8 cups to 2 servings			
5.) Write the ratio as a fraction simplest form:  50 cars to 100 trucks	6.) Write the ratio as a fraction simplest form: 9 pencils to 11 pens			

## Unit: NUMBER RELATIONSHIPS and COMPUTATION **Objective:** Compare and order fractions and decimals. Ordering fractions only: Ordering fractions and decimals: 1) determine the least common denominator (LCD) 1) Change the fractions to decimals of the fractions 2) Compare the decimals 2) rewrite each fraction as an equivalent fraction using the LCD EX: order the numbers 0.3; $\frac{3}{8}$ ; and 0.38 from Compare the numerators least to greatest EX: order the fractions $\frac{1}{2}$ ; $\frac{3}{8}$ ; $\frac{7}{12}$ from least to greatest 8)3.000 1) $\frac{3}{8} = 0.375$ 1) LCD of 2, 8, and 12 is 24 $\frac{3}{8} = \frac{9}{24}$ 60 -5640 - 40 2) Compare the decimals: 0.3 < 0.375 < 0.38 3) Comparing the numerators: **Therefore:** $0.3 < \frac{3}{8} < 0.38$ 1.) 2.) Order the fractions $\frac{2}{3}$ ; $\frac{5}{6}$ ; $\frac{3}{4}$ from least to greatest Order the numbers 0.78; $\frac{3}{4}$ ; and 0. 8 from least to greatest 3.) Order the fractions $\frac{3}{5}$ ; $\frac{7}{10}$ ; $\frac{5}{6}$ from least to greatest Order the numbers $\frac{3}{10}$ ; $\frac{1}{5}$ ; and 0.25 from least to greatest 5.) Which number has the greatest value? 0.94; $\frac{19}{20}$ ; or $\frac{24}{25}$ Order the fractions $\frac{1}{2}$ ; $\frac{5}{9}$ ; $\frac{5}{6}$ from least to greatest

## Unit: NUMBER RELATIONSHIPS and COMPUTATION

**Objective:** Add and subtract fractions and mixed numbers and express answers in simplest form.

## **Adding and Subtracting Fractions:**

- 1) determine the least common denominator (LCD) of the fractions
- 2) rewrite each fraction as an equivalent fraction using the LCD
- 3) Add or subtract the fractions
- 4) Simplify if necessary

EX: Add 
$$\frac{1}{2} + \frac{3}{8}$$

- 1) LCD of 2 and 8 is 8
- 2)  $\frac{1}{2} = \frac{4}{8}$  $+ \frac{3}{8} = \frac{3}{8}$
- 3)  $\frac{7}{8}$
- 4) (can't be simplified)

- **EX:** Subtract  $3\frac{3}{5} 1\frac{1}{6}$ 
  - 1) LCD of 5 and 6 is 30
  - 2)  $3\frac{3}{5} = 3\frac{18}{30}$  $-1\frac{1}{6} = -1\frac{5}{30}$ 
    - 3)  $2\frac{13}{30}$
  - 4) (can't be simplified)

1.) 
$$\frac{4}{6} + \frac{1}{3} =$$

2.)  $\frac{11}{12} - \frac{5}{8} =$ 

3.) 
$$1\frac{3}{8} + 2\frac{3}{4} =$$

- 4.)  $3\frac{5}{6} 1\frac{4}{5} =$
- 5.) Shelly has two pieces of yarn. One is  $1\frac{1}{2}$  yards long and the other is  $2\frac{3}{4}$  yards long. How much yarn does she have altogether?
- 6.) Marty weighs 64 ¼ pounds and Nathan weighs 76 ½ pounds. How much more does Nathan weigh than Marty?

## 7th Grade - Summer Math Packet

## Unit: NUMBER RELATIONSHIPS and COMPUTATION

**Objective:** Multiply fractions and mixed numbers and express answers in simplest form.

## **Multiplying Fractions and Mixed Numbers:**

- 1) Change Mixed numbers to improper fractions
- 2) Multiply numerators
- 3) Multiply denominators
- 4) Simplify if necessary

**EX:** multiply 
$$\frac{1}{2} \times \frac{3}{8}$$

1) No mixed numbers

2) 
$$\frac{1}{2} \times \frac{3}{8} = \frac{3}{8}$$

- 3)  $\frac{1}{2} \times \frac{3}{8} = \frac{3}{16}$
- 4) (can't be simplified)

**EX:** Multiply 
$$\frac{1}{3} \times 6\frac{3}{7}$$

1)  $6\frac{3}{7} = \frac{45}{7}$  as an improper fraction

2) 
$$\frac{1}{3} \times \frac{45}{7} = \frac{45}{7}$$

- 3)  $\frac{1}{3} \times \frac{45}{7} = \frac{45}{21}$
- **4)** Simplified:  $\frac{45}{7} = 2\frac{1}{7}$

1.) 
$$\frac{5}{6} \times \frac{1}{2} =$$

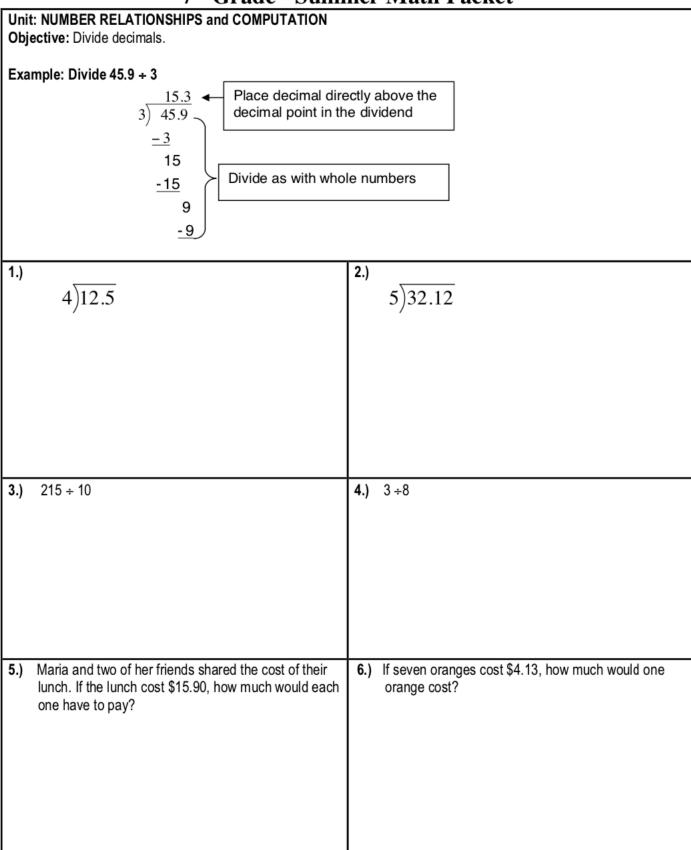
**2.)** 
$$\frac{9}{10} \times \frac{2}{3} =$$

3.) 
$$2\frac{1}{2} \times 1\frac{2}{5} =$$

**4.)** 
$$2\frac{1}{4} \times 3\frac{1}{3} =$$

- **5.)** Belinda lives 1 ½ times further from school than Jamie does. If Jamie lives 4 1/5 miles from school, how far does Belinda live?
- **6.)** Mario practices his guitar every day for ¾ of an hour. How long does he practice for week?

Unit: NUMBER RELATIONSHIPS and COMPUTATION Objective: Multiply decimals.			
Examples: Multiply 3.4 X 1.2  3.4  X 1.2  6 8  — multiply 34 by 2 (ignore the decimal point)  + 3 4 0  — multiply 34 by 10 (the 1 is in the tens place  4 0 8  — add 68 and 340  Count the number of decimal places in the original  Since there are 2 total decimal places, the answer shave 2 decimal places.	) 3.4 (1 decimal place) problem. X1.2 (1 decimal place)		
Answer 4.08			
<b>1.)</b> 1.2 X 0.5	<b>2.)</b> 3.3 × 4.6		
3.) 0.4 × 0.6	<b>4.)</b> 7.89 X 5		
5.) Turkey cost \$5.79 a pound. How much will 2.9 pounds of turkey cost? Round to the nearest cent.	<b>6.)</b> Ralph bought 6 CDs at a cost of 17.75 each. How much did the CDs cost altogether?		



Unite NUMBER RELATIONSCHIPS and COMPUTATION		
Unit: NUMBER RELATIONSHIPS and COMPUTATION Objective: Determine 10, 20, 25, or 50 percent of a whole number.		
Example: Determine 25% of 40		
Method 1: Change the percent to a fraction and multiply	Method 2: Change the percent to a decimal and multiply	
25%= 1/4	25%= 0.25 40 x 0.25	
$\frac{1}{4} \times 40 = 10$	0.25 X 40 = 10.00 200 +800	
4 Therefore 25% of 40 is 10.	Therefore 25% of 40 is 10.	
1.) Determine 20% of 65.	2.) Determine 50% of 120.	
3.) Determine 25% of 20.	4.) Determine 10% of 35.	
5.) 20% of the 250 students ate pizza for lunch. How many students ate pizza?	6.) Nia saved 10% on her CD purchase. If the CD originally cost \$24.90, how much did she save?	

#### Unit: NUMBER RELATIONSHIPS and COMPUTATION

**Objective:** Use the distributive property to simplify numeric expressions using whole numbers.



Examples: 
$$42 \times 5 = (40 \times 5) + (2 \times 5)$$
  
 $42 = 40 + 2$ 

Which of these expressions is equivalent to 15 x 28?

- a)  $(15 \times 20) + (15 \times 8)$
- b)  $(15 \times 8) + (28 \times 10)$
- c)  $(15 \times 10) + (28 \times 10)$
- d)  $(28 \times 15) + (10 \times 10)$

2.)

Which of these expressions is equivalent to 31 x 14?

- a)  $(10 \times 30) + (4 \times 1)$
- b)  $(14 \times 1) + (14 \times 30)$
- c)  $(10 \times 1) + (30 \times 4)$
- d)  $(30 \times 14) + (10 \times 14)$

3.)

1.)

Which of these expressions is **NOT** equivalent to 21 x 13?

- a)  $(13 \times 20) + (13 \times 1)$
- b)  $(21 \times 10) + (21 \times 3)$
- c)  $(30 \times 13) (9 \times 13)$
- d)  $(20 \times 10) + (1 \times 3)$

4.)

Which of these expressions is **NOT** equivalent to  $37 \times 21$ ?

- a)  $(21 \times 30) + (21 \times 7)$
- b)  $(30 \times 20) + (7 \times 1)$
- c)  $(40 \times 21) (3 \times 21)$
- d)  $(37 \times 20) + (37 \times 1)$

5.)

Which of these expressions is equivalent to 34 x 12?

- a)  $(30 \times 10) + (4 \times 2)$
- b)  $(34 \times 10) + (34 \times 12)$
- c)  $(30 \times 12) + (4 \times 12)$
- d) (30 x 12) (4 x 12)

6.)

Which of these expressions is **NOT** equivalent to 49 x 19?

- a)  $(40 \times 19) + (9 \times 19)$
- b) (49 x 20) (49 x 1)
- c) (50 x 19) (1 x 19)
- d)  $(49 \times 10) + (9 \times 9)$

Unit: NUMBER RELATIONSHIPS and COMPUTATION Objective: Estimate to determine the product of a decimal and a whole number			
Example: Multiply 6.45 X 7			
1. Round to the nearest whole numbers.	6.45 rounds to 6 Since 7 is already a whole number, it stays the same.		
2. Multiply the rounded numbers	6 X 7		
3. Answer	42		
Estimate each of the following multiplicat	ion problems. I	Round a	all decimals to the nearest whole number.
1.) 6 X 1.65	•		0.82 X 4
3.) 3 X 9.95		4.) 12	2.9 X 7
5.) Three pairs of shoes are priced at \$3 Estimate the total cost for the all 3 periods.			If you work 6 hours at \$6.35 an hour, estimate how much you would make?

IL 'L NUMBER RELATIONOUIRO - LOOMBUTATION	
Unit: NUMBER RELATIONSHIPS and COMPUTATION Objective: Estimate to determine the quotient of a decimal.	
Example: Divide 45.9 + 10	10)50
Estimate to the nearest tens.     45.9 rounds to 50     10 stays the same	10)50
2. Divide with estimated numbers.	
3. Answer.	5
Estimate each of the following division problems. Round	
35)196.5	(2.) $(14)37.1$
2) 740 44	4) 00 004 24
<b>3.)</b> 7.49 ÷ 14	<b>4.)</b> 89.904 ÷34
5.) Maria and twelve of her friends shared the cost of their lunch. If the lunch cost \$75.90, estimate how much would each one have to pay?	6.) Brianna and 15 of her friends bought sodas after their lacrosse game. If the drinks cost \$43.29, estimate how much each person would owe if the cost is divided equally?